

1. Solve the following IVP,

$$\begin{cases} y''(t) + 8y'(t) + 16y(t) = 0 \\ y(0) = 2, \quad y'(0) = -3. \end{cases}$$

$$\text{ch. eq : } r^2 + 8r + 16 = 0 \quad \Leftrightarrow (r+4)^2 = 0$$

$$\therefore r = -4, -4 \quad (\text{double root})$$

$$\therefore y = c_1 e^{-4t} + c_2 t e^{-4t}$$

$$y' = -4c_1 e^{-4t} + c_2 e^{-4t} - 4c_2 t e^{-4t}$$

$$y(0) = 2 \rightarrow c_1 = 2$$

$$y'(0) = -3 \rightarrow -4c_1 + c_2 = -3$$

$$\left. \begin{array}{l} -8 + c_2 = -3 \\ \therefore c_2 = 5 \end{array} \right\}$$

$$\therefore c_2 = 5$$

$$\therefore y(t) = 2e^{-4t} + 5te^{-4t}$$

Answer:

$$2e^{-4t} + 5te^{-4t}$$